Index

absolute convergence of an infinite product, 6-2
absolute value, 1-1
analytic continuation, 4-41
analytic continuation along a curve, 4-41
analytic function, 1-4
analytic k-th root, 3-8
analytic logarithm, 3-4
analytic mappings of one disk to another, 4-21ff.
angle-preserving property, 4-19
annulus, 4-1
argument, 1-1, 3-1
argument principle, 4-9
argument principle for meromorphic functions, 4-10
Bezout domain, 6-13
big Picard theorem, 4-5
bounded family of functions, 5-3
Casorati-Weierstrass theorem, 4-4
Cauchy's estimate, 2-21
Cauchy's integral formula, 3-9, 3-11
Cauchy's integral formula for a circle, 2-12
Cauchy's theorem, 3-9, 3-18 (homology version), 5-11 (homotopic version)
Cauchy's theorem for starlike regions, 2-6, 2-9
Cauchy's theorem for triangles, 2-5, 2-8
Cauchy kernel, 4-25
Cauchy-Riemann equations, 1-6
closed curve or path, 2-2
compactness criterion, 5-5
complex-differentiability, 1-4
conformal equivalence, 5-10
conformal map, 4-20
conjugate, 1-2
continuous argument, 3-2
continuous logarithm, 3-2
convergence of an infinite product, 6-1
convex set, 1-3
cosine function, 2-20
curve, 2-2
cycle, 3-11
derivative, 1-4
direct analytic continuation, 4-41
Dirichlet problem, 4-27, 4-28, 5-28
distance, 1-2
dog-walking theorem, 3-7, 3-8
Enestrom’s theorem, 1-9
equicontinuous family of functions, 5-3
equivalent function elements, 4-42
essential singularity, 4-3
Euler’s product formula, 7-2
expanding conformal maps to the boundary, 5-18ff.
exponential function, 1-8, 2-19
extended complex plane, 3-13
finitely generated ideal, 6-13
function element, 4-41
fundamental theorem for integrals on paths, 2-3
fundamental theorem of algebra, 2-21
generalized analytic function, 4-42
greatest common divisor, 6-12
harmonic conjugate, 1-9, 5-12
harmonic function, 1-8
Harnack’s inequality, 4-30
hexagon lemma, 3-16
holomorphic function, 1-4
homologous curves and cycles, 3-15, 5-11
homotopic curves, 4-42
homotopy, 4-42, 5-11
Hurwitz’s theorem, 5-2
hyperbolic functions, 2-20
ideal, 6-13
identity theorem, 2-23
identity theorem for harmonic functions, 2-25
index, 3-5
infinite products, 6-1ff.
integral, 2-1, 2-2
integral of the Cauchy type, 2-13
isolated singularity, 4-1
isolated singularity at infinity, 4-5
Jensen’s formula, 4-33, 4-36
Laplace’s equation, 1-8
Laurent expansion, 4-3
Laurent series, 4-2
law of permanence of functional equations, 4-45
length of a path, 2-2
L’Hospital’s rule, 2-26
linear fractional transformation, 4-17, 4-18
Liouville’s theorem, 2-21
logarithm, 3-1
logarithmic derivative, 3-4
magnitude, 1-1
M-L theorem, 2-3
maximum and minimum principles for harmonic functions, 2-25
maximum principle, 2-23, 2-24
meromorphic function, 4-6, 6-9
minimum principle, 2-24
Mittag-Leffler’s theorem, 6-10
Möbius transformations, 4-17
modulus, 1-1
monodromy theorem, 4-43
Montel’s theorem, 5-5
Morera’s theorem, 2-14
Noetherian ring, 6-14
open mapping theorem, 4-15
parallelogram law, 1-9
partial fraction expansion, 4-6
path, 2-2
path integral, 2-2
Poisson integral formula, 4-26, 4-27
Poisson integral formula for harmonic functions, 4-29
Poisson kernel, 4-25
Poisson-Jensen formula, 4-32
polarization, 2-1
pole, 4-3
polygonally connected, 1-3
power series, 2-11
prime number theorem, 7-1ff.
primitive, 2-3
principal branch, 3-2
principal ideal, 6-13
principal ideal domain, 6-13
punctured disk, 4-1
ratio test, 2-10
real-differentiability, 1-6
region, 1-3
relatively compact, 5-5
relatively prime, 6-12
removable singularity, 4-3
residue, 4-7
residue theorem, 4-8
Riemann hypothesis, 7-5
Riemann integral, 2-1
Riemann mapping theorem, 5-8ff.
Riemann sphere, 3-13
Riemann zeta function, 7-2
root test, 2-10
Rouche’s theorem, 4-10
Runge’s theorem, 5-13, 5-17
Schwarz’s lemma, 2-26
Schwarz reflection principle, 2-15
second Cauchy theorem, 3-18
separated sets, 1-3
series, 2-10
simple boundary point, 5-20
simple pole, 4-3
simply connected (homologically), 3-19, 5-12
simply connected (homotopically), 4-44, 5-12
sine function, 2-20
singularity, 4-1
star center, 1-3
starlike, 1-3
Tauberian theorem, 7-10
triangle inequality, 1-2
trigonometric functions, 2-20
unimodular, 2-20
unit, 6-12
Vitali’s theorem, 5-6
von Mangoldt function, 7-5
Weierstrass factorization theorem, 6-7
Weierstrass M-test, 2-11
Weierstrass products, 6-5
winding number, 3-5
zero set, 2-22