

MATH 220

Test 3

Spring 2019

Name \_\_\_\_\_

NetID \_\_\_\_\_

UIN \_\_\_\_\_

Circle your TA discussion section.

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|--|---|
| ▷ AD1, TR 9:00-10:50, Ran Ji               | ▷ ADH, TR 3:00-3:50, Mina Nahvi           |
| ▷ AD2, TR 1:00-2:50, Cassie Christenson    | ▷ ADJ, TR 9:00-9:50, Yuxuan "Yuki" Zhang  |
| ▷ AD3, TR 11:00-12:50, Dana Neidinger      | ▷ ADK, TR 10:00-10:50, Souktik Roy        |
| ▷ ADA, TR 8:00-8:50, Eion Blanchard        | ▷ ADL, TR 11:00-11:50, Gidon Orelowitz    |
| ▷ ADB, TR 9:00-9:50, Eion Blanchard        | ▷ ADM, TR 12:00-12:50, Vincent Villalobos |
| ▷ ADC, TR 10:00-10:50, Yuxuan "Yuki" Zhang | ▷ ADN, TR 1:00-1:50, Kesav Krishnan       |
| ▷ ADD, TR 11:00-11:50, Stathis Chrontsios  | ▷ ADO, TR 2:00-2:50, Stathis Chrontsios   |
| ▷ ADE, TR 12:00-12:50, Kesav Krishnan      | ▷ ADQ, TR 4:00-4:50, Mina Nahvi           |
| ▷ ADF, TR 1:00-1:50, Souktik Roy           | ▷ ADR, TR 10:00-10:50, Vincent Villalobos |
| ▷ ADG, TR 2:00-2:50, Gidon Orelowitz       |   |

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- Sit in your assigned seat (circled below).
  - Do not open the test or write formulas upon it until I say *START*.
  - Remove smartwatches and turn off all electronic devices.
  - Put away all items except a pen/pencil and an eraser.
  - Remove hats and sunglasses.
  - There is no partial credit on multiple-choice questions. For all other questions, you must show sufficient work to justify your answer.
  - While the test is in progress, we will not answer questions concerning the test material.
  - Do not leave early unless you are at the end of a row.
  - Quit working and close this test booklet when I say *STOP*.
  - Quickly turn in your test to me or a TA and show your Student ID.
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310	311	312	R	313	314	315	316	317	318	—	—	319	320	321	322	323	R	324	325	326
291	292	293	Q	294	295	296	297	298	299	300	301	302	303	304	305	306	Q	307	308	309
272	273	274	P	275	276	277	278	279	280	281	282	283	284	285	286	287	P	288	289	290
253	254	255	O	256	257	258	259	260	261	262	263	264	265	266	267	268	O	269	270	271
234	235	236	N	237	238	322	240	241	242	243	244	245	246	247	248	249	N	250	251	252
216	217	218	M	219	220	221	222	223	224	225	226	227	228	229	230		M	231	232	233
199	200	201	L	202	203	204	205	206	207	208	209	210	211	212	213		L	214	215	216
181	182	183	K	184	185	186	187	188	189	190	191	192	193	194	195		K	196	197	198
163	164	165	J	166	167	168	169	170	171	172	173	174	175	176	177		J	178	179	180
145	146	147	I	148	149	150	151	152	153	154	155	156	157	158	159		I	160	161	162
127	128	129	H	130	131	132	133	134	135	136	137	138	139	140	141		H	142	143	144
109	110	111	G	112	113	114	115	116	117	118	119	120	121	122	123		G	124	125	126
91	92	93	F	94	95	96	97	98	99	100	101	102	103	104	105		F	106	107	108
73	74	75	E	76	77	78	79	80	81	82	83	84	85	86	87		E	88	89	90
55	56	57	D	58	59	60	61	62	63	64	65	66	67	68	69		D	70	71	72
38	39	40	C	41	42	43	44	45	46	47	48	49	50	51			C	52	53	54
21	22	23	B	24	25	26	27	28	29	30	31	32	33	34			B	35	36	37
5	6	7	A	8	9	10	11	12	13	14	15	16	17				A	18	19	20
	1	2																	3	4

FRONT OF ROOM – 141 Wohlers Hall

1. (10 points) Evaluate the indefinite integral.

$$\int (91x^6 + 6 \sin x + 5 \sec^2 x + 9 \csc^2 x + 8e^x + 4) dx$$

2. (10 points) Evaluate the indefinite integral.

version 1:  $\int \sin^{80}(x) \cos^3(x) dx$

version 2:  $\int \cos^{60}(x) \sin^3(x) dx$

3. (10 points) Evaluate the indefinite integral.

$$\int 225x(15x + 4)^{28} dx$$

4. (10 points) Evaluate the indefinite integral.

$$\int \frac{8000x^{79}}{x^{160} + 400} dx$$

5. (10 points) Find the average value of the function  $f(x) = 40x^3e^{x^4}$  on the interval  $[0, 5]$ . Simplify your answer.

6. (10 points)

version 1: Determine the  $x$ -coordinate for the absolute maximum value of the following function.

$$g(x) = \int_6^{80x-5x^2} \left( \frac{1}{\sin^{20}(t) + 400} \right) dt$$

version 2: Determine the  $x$ -coordinate for the absolute minimum value of the following function.

$$g(x) = \int_9^{6x^2-132x} \left( \frac{1}{\cos^{40}(t) + 100} \right) dt$$

7. (10 points) Evaluate the following limit. Be sure to use proper notation throughout your evaluation of this limit. Simplify your answer.

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \frac{4 + 18kn^4}{n^6} \right)$$

8. (10 points) Suppose that  $f(x)$  is a polynomial which satisfies the following conditions.

- $\int_5^{129} f(x) dx = 30$
- $\int_{42}^{129} f(x) dx = 38$

Evaluate the following quantities.

(a)  $\int_5^{42} (2f(x) + 10) dx$

(b)  $\int_1^5 6x^2 f(x^3 + 4) dx$

9. (10 points) Let  $\mathbf{R}$  be the finite region bounded by the graphs of  $y = 12x^2$  and  $y = 48x$ . These curves intersect at the origin and at the point  $(x, y) = (4, 192)$ . Revolve  $\mathbf{R}$  around the horizontal line  $y = 220$  to form a solid. In the following manner, set up but do not evaluate definite integrals which represent the volume of the solid. Use proper notation.

(a) Integrate with respect to  $x$ .

(b) Integrate with respect to  $y$ . (The integrands in parts (a) and (b) should be different.)

10. (10 points) Given the function below, use a linear approximation to estimate  $g(1.03)$ . Simplify and write your answer in decimal form.

$$g(x) = 20 \ln(x) - 8e^{x^2-1}$$

**Students – do not write on this page!**

1. (10 points) \_\_\_\_\_

2. (10 points) \_\_\_\_\_

3. (10 points) \_\_\_\_\_

4. (10 points) \_\_\_\_\_

5. (10 points) \_\_\_\_\_

6. (10 points) \_\_\_\_\_

7. (10 points) \_\_\_\_\_

8. (10 points) \_\_\_\_\_

9. (10 points) \_\_\_\_\_

10. (10 points) \_\_\_\_\_

**TOTAL (100 points)** \_\_\_\_\_