



1. (10 points) Express  $\ln(115) - 3\ln(5)$  as a single logarithm. Now use a linear approximation to estimate its value. Simplify and write your answer in decimal form.

2. (10 points) Suppose that  $f(x)$  is an even function which satisfies the following conditions.

- $\int_0^{49} f(x) dx = 900$
- $\int_{-3}^3 f(x) dx = 300$

Evaluate the following quantities.

(a)  $\int_3^{49} (f(x) + 100) dx$

(b)  $\int_7^0 18xf(x^2) dx$

3. (10 points) Let  $g(x) = \int_{x^4+500x}^8 \frac{1}{t^{64} + 16} dt$ . Determine the  $x$ -value for the highest point on the graph of  $g(x)$ .

4. (10 points) Evaluate the following limit. Be sure to use proper notation throughout your evaluation of this limit. Simplify your answer.

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \left( \frac{54k^2 + 48nk + 5}{n^3} \right)$$

5. (10 points) Let  $\mathbf{R}$  be the finite region bounded by the graphs of  $y = 4x^2$  and  $y = 32x$ . These curves intersect at the origin and at the point  $(x, y) = (8, 256)$ . Revolve  $\mathbf{R}$  around the vertical line  $x = 10$  to form a solid. In the following manner, set up but do not evaluate definite integrals which represent the volume of the solid. Use proper notation.

(a) Integrate with respect to  $x$ .

(b) Integrate with respect to  $y$ . (The integrands in parts (a) and (b) should be different.)

6. (10 points) At time  $t$  hours, a population of bacteria is growing at a rate of  $8t + 5$  bacteria per hour. If the population is 2500 at time  $t = 4$ , then what is the population at time  $t = 6$  hours?

7. (10 points) Find the average value of the function  $f(x) = \frac{96}{\sqrt{12x + 25}}$  on the interval  $[-2, 2]$ . Simplify your answer.

8. (10 points) Evaluate the indefinite integral.

$$\int \left( 91x^6 + 42 + \frac{9}{x} + \csc^2(x) + \csc(x) \cot(x) \right) dx$$

9. (10 points) Evaluate the indefinite integral.

$$\int \sin^3(x) \cos^{93}(x) dx$$

10. (10 points) Evaluate the indefinite integral.

$$\int \frac{126e^{42x}}{e^{84x} + 1} dx$$

**Students – do not write on this page!**

1. (10 points) \_\_\_\_\_

2. (10 points) \_\_\_\_\_

3. (10 points) \_\_\_\_\_

4. (10 points) \_\_\_\_\_

5. (10 points) \_\_\_\_\_

6. (10 points) \_\_\_\_\_

7. (10 points) \_\_\_\_\_

8. (10 points) \_\_\_\_\_

9. (10 points) \_\_\_\_\_

10. (10 points) \_\_\_\_\_

**TOTAL (100 points)** \_\_\_\_\_