

1. (8 points) Find $g'(x)$ given that $g(x) = 10 \arcsin x + 4 \csc(x) - 120 \ln(x) + 6x^8$

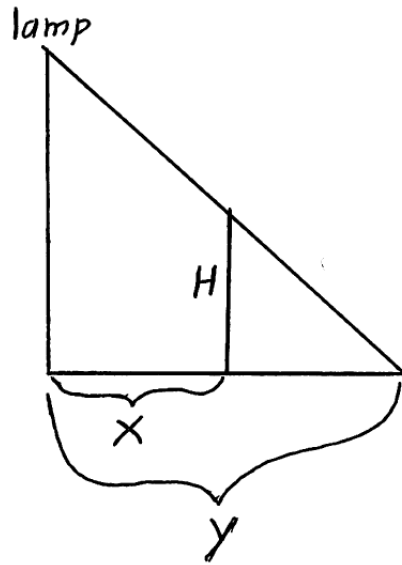
2. (8 points) Find $\frac{dw}{dt}$ given that $w = t^7 e^{5t}$

3. (8 points) Find $p'(v)$ given that $p(v) = \cos(\sqrt{v^9 + 5v})$

4. (8 points) Find $w'(q)$ given that $w(q) = \frac{\cot(5q)}{q^3 + 4}$

5. (8 points) Find $\frac{dy}{dx}$ given that $x^4 e^y = 5x^7 + 2y^3 + 42$. It is okay to leave your answer in terms of both x and y .

6. (8 points) As Nancy walks away from a 700 *cm* lamppost, the tip of her shadow moves 40% faster than she does. What is Nancy's height?



7. (12 points) Solve the following differential equations given that the graph of each solution goes through the point $(\theta, \alpha) = (0, 24)$. You must use the given variables.

(a) $\frac{d\alpha}{d\theta} = 16\alpha$

(b) $\frac{d\alpha}{d\theta} = 16\theta$

8. (10 points) Upon which interval is the function $f(x) = 7x^4 - 4x^3 + 243$ increasing?

9. (10 points) Evaluate the following limit. Simplify your answer.

$$\lim_{x \rightarrow 0} \frac{e^{8x} - 8x - 1}{1 - \cos(3x)}$$

10. (10 points) A function $f(x)$ is continuous at each real number and it has the following second derivative.

$$f''(x) = 12(e^x + 19)(x - 5)^8(x - 2)^6(x + 5)^7$$

(a) State each interval upon which the graph of $f(x)$ is concave down.

(b) State each interval upon which the graph of $f(x)$ is concave up.

(c) State each x -value at which the graph of $f(x)$ has an inflection point.

11. (10 points) Suppose $y = \frac{8}{x^6}$ for $x > 0$. Determine the x -coordinate for the point on this curve which is closest to the origin.

Students – do not write on this page!

1. (8 points) _____

2. (8 points) _____

3. (8 points) _____

4. (8 points) _____

5. (8 points) _____

6. (8 points) _____

7. (12 points) _____

8. (10 points) _____

9. (10 points) _____

10. (10 points) _____

11. (10 points) _____

TOTAL (100 points) _____