

1. (12 points) Let $f(x) = x^3 - 42x$.

Use the definition of a derivative as a limit to prove that $f'(x) = 3x^2 - 42$.

Show each step in your calculation and be sure to use proper terminology in each step of your proof.

2. (12 points) The function $f(x) = 20e^{5x} + 15x - 12$ has derivative $f'(x) = 100e^{5x} + 15$. Determine a formula for the line which is tangent to the graph of $f(x)$ at its y -intercept.

3. (12 points) Let $R(t)$ be the number of rabbits living on Lady Tottington's estate t months after they were initially discovered. This rabbit population grows exponentially. Given that $R(2) = 10$ and $R(5) = 90$, determine a formula for $R(t)$.

4. (12 points) Determine a formula for $g^{-1}(x)$ given that $g(x) = \frac{8x^9 - 3}{5x^9 + 4}$

5. (12 points) Solve the following equation for x and simplify your answer.

$$\ln(2) + 9 \ln(-x) = \ln(-128x^7)$$

6. (10 points) Suppose that $w(x)$ is odd, one-to-one, and its graph goes through the point $(4, -1/3)$.

(a) Determine another point which must be on the graph of $w(x)$.

(b) Determine a point which must be on the graph of $w^{-1}(x)$.

7. (5 points) Given that $\cos(\pi/5) = \frac{1 + \sqrt{5}}{4}$, evaluate $\cos(4\pi/5)$.

8. (5 points each) Evaluate the following limits without the use of derivatives. Show sufficient justification for each answer. An answer of 'does not exist' is not sufficient. For infinite limits you must state if it is ∞ or $-\infty$.

(a) $\lim_{x \rightarrow -\infty} \frac{(2x + 1)^5}{4 + 3x^5}$

$$(b) \lim_{x \rightarrow \infty} \frac{\cos(2x)}{x^{10}}$$

$$(c) \lim_{x \rightarrow -\infty} \frac{16 \arctan(5x) + 14\pi}{4 \arctan(9x) + 5\pi}$$

$$(d) \lim_{x \rightarrow \ln 9} \frac{e^x - 9}{e^{2x} - 81}$$

$$(e) \lim_{x \rightarrow 8^+} \frac{\ln(1/x^2)}{1 - e^{(x^2 - 64)}}$$

Students – do not write on this page!

1. (12 points) _____

2. (12 points) _____

3. (12 points) _____

4. (12 points) _____

5. (12 points) _____

6. (10 points) _____

7. (5 points) _____

8a. (5 points) _____

8b. (5 points) _____

8c. (5 points) _____

8d. (5 points) _____

8e. (5 points) _____

TOTAL (100 points) _____