

1. (5 points) Find $f'(x)$ given that $f(x) = 5x^4 + 2 \sec x - 4 \cot x + 2e^x + 4 \ln x$

2. (5 points) Find $f'(x)$ given that $f(x) = \cos(x^3 + 2)$

3. (5 points) Find $f'(x)$ given that $f(x) = \frac{e^{5x}}{x^3}$

4. (5 points) Find $f'(x)$ given that $f(x) = x^5 \arctan x$

5. (5 points) Find $f'(x)$ given that $f(x) = \tan(\ln(\sin(3x)))$

6. (12 points) Find $\frac{dy}{dx}$ given that $x^5y^2 = 6x + 4y$

7. (12 points) Find the equation of the line tangent to the curve $f(x) = 5x^2 + 2x + 3$ at $x = 1$. Write your simplified answer in the form $y = mx + b$.

8. (12 points) Solve the following differential equations given that the graph of each solution goes through the point $(p, w) = (1, 8)$. You must use the given variables.

(a) $\frac{dw}{dp} = 6p$

(b) $\frac{dw}{dp} = 6w$

9. (4 points each) Circle the correct limit. No partial credit. You do not need to show any work.

(a) $\lim_{x \rightarrow \infty} \frac{2 \ln x}{\sqrt[3]{x}}$

- (a) $-\infty$ (b) -2 (c) -1 (d) 0 (e) 1 (f) 2 (g) ∞

(b) $\lim_{x \rightarrow 0} \frac{e^{10x} - 1}{5x}$

- (a) $-\infty$ (b) -2 (c) -1 (d) 0 (e) 1 (f) 2 (g) ∞

(c) $\lim_{x \rightarrow \infty} \frac{e^{10x} - 1}{5x}$

- (a) $-\infty$ (b) -2 (c) -1 (d) 0 (e) 1 (f) 2 (g) ∞

(d) $\lim_{x \rightarrow \pi} \frac{2 \cos x}{(\pi - x)^2}$

- (a) $-\infty$ (b) -2 (c) -1 (d) 0 (e) 1 (f) 2 (g) ∞

(e) $\lim_{x \rightarrow 3} \frac{e^{x-3} + 1}{2x - 5}$

- (a) $-\infty$ (b) -2 (c) -1 (d) 0 (e) 1 (f) 2 (g) ∞

10. (10 points) State the interval upon which the graph of $f(x) = \ln(x - 4) + \ln(10 - x)$ is increasing and the interval upon which it is decreasing.

11. (9 points) For each $x > 0$, a line goes through the point $(0, 0)$ and a point on the curve $y = x^4 e^{-8x}$. Which value of x gives the line with largest slope?

Students – do not write on this page!

1. (5 points) _____

2. (5 points) _____

3. (5 points) _____

4. (5 points) _____

5. (5 points) _____

6. (12 points) _____

7. (12 points) _____

8. (12 points) _____

9. (20 points) _____

10. (10 points) _____

11. (9 points) _____

TOTAL (100 points) _____