

1. (2 points) Find the domain of the function  $f(x) = \sqrt{50 - 2x} + \ln(x - 8)$ .

$$50 - 2x \geq 0 \quad \text{and} \quad x - 8 > 0$$

$$50 \geq 2x$$

$$x > 8$$

$$25 \geq x$$

$$8 < x \leq 25$$

or

$$(8, 25]$$

2. (2 points) Suppose that  $f(x) = \frac{1}{x^2 - 4}$  and  $g(x) = \frac{1}{x} + 5$ .

- (a) Find a simplified formula for  $(g \circ f)(x)$ .

$$(g \circ f)(x) = g(f(x))$$

$$= g\left(\frac{1}{x^2 - 4}\right)$$

$$x \neq 2, x \neq -2$$

$$= \frac{1}{1/(x^2 - 4)} + 5$$

$$= x^2 - 4 + 5$$

$$= x^2 + 1$$

- (b) Find the domain of  $(g \circ f)(x)$ .

all real numbers except  $\pm 2$

or

$$(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$$

3. (3 points) Given that  $f(x)$  is an even function and that  $g(x) = (f(x) + 5)^3$ , is  $g(x)$  an odd function, an even function or neither? Give a clear justification for your answer.

$$\begin{aligned} g(-x) &= (f(-x) + 5)^3 \\ &= (f(x) + 5)^3 \quad \text{since } f \text{ is even} \\ &= g(x) \end{aligned}$$

$g$  is an even function

4. (3 points) Carefully sketch the graph of  $y = 5 + 2e^{-x}$ . If there are any horizontal or vertical intercepts or asymptotes, then their locations should be accurately shown on your graph.

