

## MATH 220

## Test 1

Fall 2019

Name \_\_\_\_\_

NetID \_\_\_\_\_

Circle your TA discussion section.

UIN \_\_\_\_\_

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| ▷ <b>AD1</b> , TR 11:00-12:50, Mina Nahvi        | ▷ <b>ADJ</b> , TR 9:00-9:50, Robert "Bob" Krueger  |
| ▷ <b>AD2</b> , TR 9:00-10:50, Adriana Morales    | ▷ <b>ADK</b> , TR 10:00-10:50, Sarah Simpson       |
| ▷ <b>AD3</b> , TR 1:00-2:50, Vincent Villalobos  | ▷ <b>ADL</b> , TR 11:00-11:50, Rocco Davino        |
| ▷ <b>AD@</b> , TR 9:00-9:50, Phuong "Sophie" Le  | ▷ <b>ADM</b> , TR 12:00-12:50, Dara Zirlin         |
| ▷ <b>ADA</b> , TR 8:00-8:50, Scott Harman        | ▷ <b>ADN</b> , TR 1:00-1:50, John "Connor" Grady   |
| ▷ <b>ADB</b> , TR 9:00-9:50, Lutian Zhao         | ▷ <b>ADO</b> , TR 2:00-2:50, Shuyu "Sonya" Xiao    |
| ▷ <b>ADC</b> , TR 10:00-10:50, Lutian Zhao       | ▷ <b>ADQ</b> , TR 10:00-10:50, Saaber Pourmotabbed |
| ▷ <b>ADD</b> , TR 11:00-11:50, Dara Zirlin       | ▷ <b>ADR</b> , TR 9:00-9:50, Scott Harman          |
| ▷ <b>ADE</b> , TR 12:00-12:50, David Altizio     | ▷ <b>ADS</b> , TR 12:00-12:50, Rocco Davino        |
| ▷ <b>ADF</b> , TR 1:00-1:50, Saaber Pourmotabbed | ▷ <b>ADT</b> , TR 2:00-2:50, Ryan McConnell        |
| ▷ <b>ADG</b> , TR 2:00-2:50, John "Connor" Grady | ▷ <b>ADU</b> , TR 3:00-3:50, Shuyu "Sonya" Xiao    |
| ▷ <b>ADH</b> , TR 3:00-3:50, Sarah Simpson       | ▷ <b>ADW</b> , TR 8:00-8:50, Robert "Bob" Krueger  |
| ▷ <b>ADI</b> , TR 4:00-4:50, Ryan McConnell      |  |

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- Sit in your assigned seat (circled below).
  - Do not open this test booklet until I say *START*.
  - Turn off all electronic devices and put away all items except a pen/pencil and an eraser.
  - Remove hats and sunglasses.
  - There is no partial credit on multiple-choice questions. For all other questions, you must show sufficient work to justify your answer.
  - While the test is in progress, we will not answer questions concerning the test material.
  - Do not leave early unless you are at the end of a row.
  - Quit working and close this test booklet when I say *STOP*.
  - Quickly turn in your test to me or a TA and show your Student ID.
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310	311	312	R	313	314	315	316	317	318	—	—	319	320	321	322	323	R	324	325	326
291	292	293	Q	294	295	296	297	298	299	300	301	302	303	304	305	306	Q	307	308	309
272	273	274	P	275	276	277	278	279	280	281	282	283	284	285	286	287	P	288	289	290
253	254	255	O	256	257	258	259	260	261	262	263	264	265	266	267	268	O	269	270	271
234	235	236	N	237	238	322	240	241	242	243	244	245	246	247	248	249	N	250	251	252
216	217	218	M	219	220	221	222	223	224	225	226	227	228	229	230		M	231	232	233
199	200	201	L	202	203	204	205	206	207	208	209	210	211	212	213		L	214	215	216
181	182	183	K	184	185	186	187	188	189	190	191	192	193	194	195		K	196	197	198
163	164	165	J	166	167	168	169	170	171	172	173	174	175	176	177		J	178	179	180
145	146	147	I	148	149	150	151	152	153	154	155	156	157	158	159		I	160	161	162
127	128	129	H	130	131	132	133	134	135	136	137	138	139	140	141		H	142	143	144
109	110	111	G	112	113	114	115	116	117	118	119	120	121	122	123		G	124	125	126
91	92	93	F	94	95	96	97	98	99	100	101	102	103	104	105		F	106	107	108
73	74	75	E	76	77	78	79	80	81	82	83	84	85	86	87		E	88	89	90
55	56	57	D	58	59	60	61	62	63	64	65	66	67	68	69		D	70	71	72
38	39	40	C	41	42	43	44	45	46	47	48	49	50	51			C	52	53	54
21	22	23	B	24	25	26	27	28	29	30	31	32	33	34			B	35	36	37
5	6	7	A	8	9	10	11	12	13	14	15	16	17				A	18	19	20
	1	2																3	4	

FRONT OF ROOM – 141 Wohlers Hall

1. (10 points) Let  $f(x) = 5x - 21x^2$ .

Use the definition of a derivative as a limit to prove that  $f'(x) = 5 - 42x$ .

Show each step in your calculation and be sure to use proper terminology in each step of your proof.

2. (10 points) Determine all values of  $x$  which satisfy the equation below.

$$3 \ln(5) + e^{2 \ln(4-3x)} = \ln(125e^{241-24x})$$

3. (10 points) Find an equation for each horizontal asymptote on the graph of the function  $f(x)$ .

$$f(x) = \begin{cases} 20 \arctan(x) + 52\pi & \text{if } x < 0 \\ 80e^{-2x} - 5 & \text{if } x \geq 0 \end{cases}$$

4. (10 points) The function  $f(x) = 4e^{8x} - 2x + 1$  has derivative  $f'(x) = 32e^{8x} - 2$ . Determine a formula for the line which is tangent to the graph of  $f(x)$  at its  $y$ -intercept.

5. (10 points) The function  $R(x) = \frac{9e^{3x}}{5 + 2e^{3x}}$  is one-to-one. Find a formula for its inverse  $R^{-1}(x)$ .

6. (10 points) Use interval notation to state the domain of the given function.

$$f(x) = \frac{\cos(x^2 - 121)}{x - \sqrt{42 - x}}$$

7. (8 points each) Evaluate the following limits and write your answers in simplified form. For infinite limits, you must clearly show whether the limit is  $\infty$  or  $-\infty$ . We will learn l'Hospital's Rule and other shortcuts for obtaining limits later. For now you are not allowed to use these approaches.

(a)  $\lim_{x \rightarrow \infty} \frac{8 + 9x^{1/6}}{2x^{1/6} + 3}$

$$(b) \lim_{x \rightarrow \infty} \frac{8 \sin(x) + 20}{x^{42}}$$

$$(c) \lim_{x \rightarrow 9/5} \frac{25x^2 - 81}{5x - 9}$$

$$(d) \lim_{x \rightarrow 196^-} \frac{\sqrt{x} + 7}{\sqrt{x} - 7}$$

$$(e) \lim_{x \rightarrow 8^+} \frac{9e^{-5x}}{\ln(8/x)}$$

**Students – do not write on this page!**

1. (10 points) \_\_\_\_\_

2. (10 points) \_\_\_\_\_

3. (10 points) \_\_\_\_\_

4. (10 points) \_\_\_\_\_

5. (10 points) \_\_\_\_\_

6. (10 points) \_\_\_\_\_

7a. (8 points) \_\_\_\_\_

7b. (8 points) \_\_\_\_\_

7c. (8 points) \_\_\_\_\_

7d. (8 points) \_\_\_\_\_

7e. (8 points) \_\_\_\_\_

**TOTAL (100 points)** \_\_\_\_\_