

Name _____

- You have 20 minutes
- No calculators
- Show sufficient work

1. (2 points) Fill in the missing information for the following two theorems.

Mean Value Theorem Let f be a function that satisfies the following two hypotheses.(1) f is _____ on the closed interval $[a, b]$.(2) f is _____ on the open interval (a, b) .Then there is a number c in (a, b) such that _____ .**Rolle's Theorem** Let f be a function that satisfies the following three hypotheses.(1) f is _____ on the closed interval $[a, b]$.(2) f is _____ on the open interval (a, b) .

(3) _____ .

Then there is a number c in (a, b) such that _____ .

2. (2 points) Evaluate the definite integral. Simplify your answer.

$$\int_1^{e^2} \frac{24}{x\sqrt{9+8\ln(x)}} dx$$

3. (2 points) Evaluate the indefinite integral.

$$\int \frac{10e^{2x} \cos(e^{2x})}{\sin^2(e^{2x}) + 1} dx$$

4. (2 points) Evaluate the indefinite integral.

$$\int \frac{4x^{11}}{(x^4 + 2)^3} dx$$

5. (2 points) Let \mathbf{R} be the finite region bounded by the given functions. In the following way, set up but do not evaluate definite integrals which represent the area of the region \mathbf{R} .

$$y = 10\sqrt{x}$$

$$y = 5x$$

- (a) Integrate with respect to x .

- (b) Integrate with respect to y . (The integrands in parts (a) and (b) should be different.)