

Name _____

- You have 20 minutes
- No calculators
- Show sufficient work

1. (2 points) Fill in the missing information for the following two theorems.

Mean Value Theorem Let f be a function that satisfies the following two hypotheses.

(1) f is _____ on the closed interval $[a, b]$.

(2) f is _____ on the open interval (a, b) .

Then there is a number c in (a, b) such that _____ .

Rolle's Theorem Let f be a function that satisfies the following three hypotheses.

(1) f is _____ on the closed interval $[a, b]$.

(2) f is _____ on the open interval (a, b) .

(3) _____ .

Then there is a number c in (a, b) such that _____ .

2. (2 points) Evaluate the definite integral. Simplify your answer.

$$\int_{\sqrt{17}}^{\sqrt{41}} \frac{10x}{\sqrt{x^2 + 8}} dx$$

3. (2 points) Evaluate the indefinite integral.

$$\int \frac{10x^4}{x^{10} + 1} dx$$

4. (2 points) Evaluate the indefinite integral.

$$\int e^{6x} (e^{3x} + 1)^{20} dx$$

5. (2 points) Let \mathbf{R} be the finite region bounded by the given functions. In the following way, set up but do not evaluate definite integrals which represent the area of the region \mathbf{R} .

$$y = e^{4x}$$

$$y = 81$$

$$x = 0$$

(a) Integrate with respect to x .

(b) Integrate with respect to y . (The integrands in parts (a) and (b) should be different.)