

1. Let  $B = \{\vec{v}_1, \vec{v}_2, \vec{v}_3\}$  be a basis of a subspace  $S$  of a vector space  $V$ . Show that  $B' = \{\vec{v}_1, \vec{v}_1 + \vec{v}_2, \vec{v}_1 + \vec{v}_2 + \vec{v}_3\}$  also forms a basis of  $S$ .
2. Let  $A$  be an  $n \times n$  invertible matrix with  $\lambda$  as its eigen values. Show that  $A^{-1}$  has  $\frac{1}{\lambda}$  as its eigen values. (Hint: Show that  $|A^{-1} - \frac{1}{\lambda}I_n| = 0$ )