Notes on “Degree estimates for polynomials constant on a hyperplane”

Note that if we apply Theorem 1, we can change the assumption in Theorem 2 to be $2N - 3 < \frac{2n-3}{3} \sqrt{n}$, hence getting an assumption that does not depend on $d$. 